Analysis of the Geographically and Temporally Weighted Regression (GTWR) of the GRDP the Construction Sector in Java Island

Sugi Haryanto 1,*, Muhammad Nur Aidi 2, Anik Djuraidah 2

1 Sub directorate of Construction Statistics at BPS-Statistics Indonesia, Jl. dr. Sutomo No. 6-8, Jakarta 10710
   Master of Applied Statistics IPB University
2 Lecturer at Statistics Department, IPB University, Jl. Meranti Wing 22 Level 4, IPB Dramaga, Bogor 16680, Indonesia
* Corresponding Author (e-mail: sugih@bps.go.id)

Received: 14 December 2018 / Accepted: 13 August 2019 / Published: 16 August 2019

Abstract. The construction sector is one of the sectors that has strategic value in the national economy of Indonesia. Economic activity in an area is measured using Gross Regional Domestic Product (GRDP), therefore the development of economic activities in the construction sector can be seen from its GRDP. The Geographically and Temporally Weighted Regression (GTWR) model is a development of the Geographically Weighted Regression (GWR) model which takes into account the diversity of locations and times. This study used secondary data, namely the GRDP of the construction sector as a response variable, and four explanatory variables, namely the size of population, local revenue, area and the number of construction establishments. The purpose of the study is to determine the factors that influence each regency/municipality each year observing the GRDP of the construction sector in Java together with the GTWR model. This model is more effective in describing the GRDP value of the construction sector of regencies/municipalities in Java Island in 2010-2016. This is indicated by the decrease in the values of Root Mean Square Error (RMSE), Mean Absolute Deviation (MAD), and the Mean Absolute Percentage Error (MAPE).

Keywords: construction, GRDP, GRDP the construction sector, GTWR, spatial


Kata kunci: konstruksi, PDRB, PDRB sektor konstruksi, GTWR, spasial
1. Introduction

Construction is an economic activity that produces goods and services related to buildings, which are integrated with the land where they are located, and used as places of residence or for other fields of activity. The construction sector has strategic value in the national economy (BPS-Statistics Indonesia, 2017). It plays an important role in national economic conditions, determined by the size of the its contribution to the growth of other business sectors. The development of the construction sector will support the creation of social and economic infrastructure, creating better accessibility, which can spur the growth of other economic sectors (Giyarsih, 2010). Infrastructure development is the focus of the government development set out in the 2015-2019 National Medium-Term Development Plan (NMTDP). It consists of various types of development projects, including the construction of roads, bridges, airports, amongst others. Based on the ministry/agency agreement only 30 projects were prioritized, most of which were located in Java. The development of the property sector, which is supported by the growth of the construction sector, can expand central economics (Wibowo et al., 2018).

The development of the construction sector needs to be monitored and evaluated with actual, accurate and continuous statistical data (BPS-Statistics Indonesia, 2016). The regional economy is said to grow and develop if the goods and services produced in a certain period are greater than in the previous period, which is then reduced to value-added. Gross Regional Domestic Product (GRDP) is one of the indicators used to measure economic activity in a region. Therefore, the development of economic activities in the construction sector can be seen from its GRDP.

Several studies on factors that influence GRDP have been conducted. Safitri and Aliasuddin (2016) found that the population had a positive and significant effect. Nasution (2010) examined the effect of PAD on the PDRB of Banten Province, with significant influential results. Putra’s (2015) research established that the area had a significant influence, but in a negative direction, while Afandi and Soesatyo’s (2014) research shows that the number of industrial manufacturers has a positive influence on GRDP.

Data based on the regional and time require analysis that considers the diversity between regions and times. Such diversity occurs due to differences in characteristics, which are influenced by culture, economy, education, thought and recreation, amongst others (Jayadinata, 1999). The development of a region involves the process of changing characteristics over time (Anisah et al., 2017). The analytical method used in the study is Geographically and Temporally Weighted Regression (GTWR), developed by Huang et al. (2010) to model housing prices in the city of Calgary (Canada) in 2002-2004. The GTWR model is a development of the Geographically Weighted Regression (GWR) method developed by Brunsdon et al. (1996), Fotheringham et al. (1996) and Fotheringham et al. (2003), which considers the elements of location and time. The results of GTWR model were regression models whose parameter values apply only to each location and each time of observation (Fotheringham et al., 2015). In GTWR, a weighting matrix element W is used, whose magnitude depends on the proximity between locations and times. The effect of weighting will be greater the closer a location or time. The weighting function used for GTWR in this paper is the Kernel Bisquare function.

The study uses GRDP data on the construction sector from 119 regencies/municipalities in Java from the period 2010] to 2016 as the response variable. The factors that will be examined for their influence on the GRDP of the construction sector are population size, local revenue (PAD), area, and the number of construction establishments. The research data has location and time dimensions, so it is possible to use the GTWR model. The benefit of this research is to provide information to regency/municipality governments in...
Java regarding the modeling of factors that affect the GRDP of the construction sector. Consequently, these governments can develop their respective policies more appropriately and evaluate them annually. The purpose of this study is to determine the factors that influence the GRDP of the construction sector in each regency/municipality in Java each year.

2. Research Method

2.1. Data

The study uses secondary data from Badan Pusat Statistik (BPS-Statistics Indonesia) and the Directorate General of Fiscal Balance (DGFB), namely the GRDP data of the construction sector as a response variable and four explanatory variables, population size, local revenue, area and the number of construction establishments. The scope of the research data is 119 regencies/municipalities in Java Island over the period 2010 to 2016. The variables used in the study are shown in Table 1.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Unit</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>GRDP of the construction sector (Y)</td>
<td>Million rupiah</td>
<td>BPS-Statistics Indonesia</td>
</tr>
<tr>
<td>Population (X₁)</td>
<td>People</td>
<td>BPS-Statistics Indonesia</td>
</tr>
<tr>
<td>Local revenue (X₂)</td>
<td>Million rupiah</td>
<td>DGFB</td>
</tr>
<tr>
<td>Area (X₃)</td>
<td>Km²</td>
<td>BPS-Statistics Indonesia</td>
</tr>
<tr>
<td>Number of Construction Establishments (X₄)</td>
<td>Establishment</td>
<td>BPS-Statistics Indonesia</td>
</tr>
</tbody>
</table>

2.2. Geographically and Temporally Weighted Regression (GTWR) Model

The Geographically and Temporally Weighted Regression (GTWR) method is a development of the GWR method, taking into account non-stationary spatiotemporal aspects in the parameter estimation, with a weighting matrix based on the distance determined from the coordinates (x, y, t) between observation i and all the other observations, according to the GWR technique (Fotheringham et al. 2015). Huang et al. (2010) formulated the GTWR model to be written as follows:

\[ y_i = \beta(0)(u_i, v_i, t_i) + \sum_{k=1}^{p} \beta_k(u_i, v_i, t_i)x_{ik} + e_i \]

where

\[ y_i = \beta(u_i, v_i, t_i) = [X^T W(u_i, v_i, t_i)X]^{-1} X^T W(u_i, v_i, t_i) \]

If the spatial distance is \( d_S = \sqrt{(u_i - u_j)^2 + (v_i - v_j)^2} \) and the temporal distance is \( d_T, \sqrt{(t_i - t_j)^2} \), then these can be combined to form a spatiotemporal distance \( d^{ST} \)

\[ d^{ST} = \lambda d_S + \mu d_T \]

where \( \lambda \) and \( \mu \) are scale factors to balance the various effects used to measure spatial and temporal distance in the metric system. If Euclid distance and decay-based distance-Gaussian functions are used to construct the spatiotemporal weight matrices, then:

\[ (d^{ST}_i)^2 = \lambda [(u_i - u_j)^2 + (v_i - v_j)^2] + \mu (t_i - t_j)^2 \]

For example, \( \tau = \mu / \lambda \) with \( \lambda \neq 0 \), so the equation obtained is as follows:
\[
\frac{(d_{ij}^{\text{ST}})^2}{\lambda} = \left( (u_i - u_j)^2 + (v_i - v_j)^2 \right) + \tau (t_i - t_j)^2 \tag{5}
\]

The parameter \( \tau \) is obtained from the criteria by minimizing the cross-validation (CV) by initializing the initial value \( \tau \), as below:

\[
CV(\tau) = \sum_{i=1}^{n} [y_i - \hat{y}_i(\tau)]^2 \tag{6}
\]

The estimator parameters \( \lambda \) and \( \mu \) can then be obtained by an iterative method based on the estimation results \( \tau \) and which results in a minimum CV.

### 2.3. Data Analysis Procedure

Analysis and modeling were conducted using the statistical program R-3.4.2. The stages of analysis in the study were as follows:

a. Conduct data exploration to obtain an overview and information about the response variable and explanatory variables used.

b. Employ a normality test for the residuals; transformation is used if they are not normal.

c. Identify patterns of relationship between response and explanatory variables using correlation analysis and multicollinearity tests of the explanatory variables.

d. Identify spatial diversity and time by:
   a. A combined and annual Breusch-Pagan test to observe spatial diversity.
   b. The boxplot method to observe temporal diversity.

The results of the multicollinearity test are shown in Table 3. VIF values lower than 10 indicate that there is no multicollinearity in the explanatory variable used. The data used are panel data, so the VIF value is calculated for each year and a combination of all years.

### 3. Results and Discussion

#### 3.1. Description

The relationship between the response and explanatory variables can be established based on Pearson correlation values, as shown in Table 2. Local revenue \( (X_2) \) is the highest correlation coefficient value between the explanatory and response variables at 0.815, while the lowest correlation is area \( (X_3) \), at -0.181. The correlation coefficient between local revenue and the GRDP of the construction sector is positive and high, as the infrastructure in many regions uses regional income and expenditure (APBD) budget funds, some of which are local revenue.

A multicollinearity test was conducted to determine the correlation between the explanatory variables used. It is performed by calculating the value of VIF (Variance Inflation Factor) with the formula

\[
VIF_k = \frac{1}{1 - R_k^2}
\]

with \( k \) being the many explanatory variables. The coefficient of determination obtained from the explanatory variable chosen as the response variable, with the other explanatory variables becoming the explanatory variables for the response variable.

The results of the multicollinearity test are shown in Table 3. VIF values lower than 10 indicate that there is no multicollinearity in the explanatory variable used. The data used are panel data, so the VIF value is calculated for each year and a combination of all years.
Table 2. Pearson correlation coefficient between explanatory and response variables

<table>
<thead>
<tr>
<th>Response Variables</th>
<th>Population</th>
<th>Local Revenue</th>
<th>Area</th>
<th>Establishments</th>
<th>n</th>
</tr>
</thead>
<tbody>
<tr>
<td>GRDP of the construction sector</td>
<td>0.424</td>
<td>0.815</td>
<td>-0.181</td>
<td>0.675</td>
<td>833</td>
</tr>
</tbody>
</table>

Table 3. Values the VIF of explanatory variables

<table>
<thead>
<tr>
<th>Year</th>
<th>Response variable</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Population</td>
</tr>
<tr>
<td>Combination</td>
<td>1.73</td>
</tr>
<tr>
<td>2010</td>
<td>1.84</td>
</tr>
<tr>
<td>2011</td>
<td>1.84</td>
</tr>
<tr>
<td>2012</td>
<td>1.75</td>
</tr>
<tr>
<td>2013</td>
<td>1.68</td>
</tr>
<tr>
<td>2014</td>
<td>1.74</td>
</tr>
<tr>
<td>2015</td>
<td>1.72</td>
</tr>
<tr>
<td>2016</td>
<td>1.64</td>
</tr>
</tbody>
</table>

Table 4. Breusch-Pagan Test Results

<table>
<thead>
<tr>
<th>Year</th>
<th>Breusch-Pagan Value</th>
<th>p-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Combination</td>
<td>64.23</td>
<td>3.74 × 10⁻¹³*</td>
</tr>
<tr>
<td>2010</td>
<td>13.09</td>
<td>0.011*</td>
</tr>
<tr>
<td>2011</td>
<td>11.36</td>
<td>0.023*</td>
</tr>
<tr>
<td>2012</td>
<td>10.54</td>
<td>0.032*</td>
</tr>
<tr>
<td>2013</td>
<td>9.99</td>
<td>0.041*</td>
</tr>
<tr>
<td>2014</td>
<td>11.27</td>
<td>0.024*</td>
</tr>
<tr>
<td>2015</td>
<td>10.66</td>
<td>0.031*</td>
</tr>
<tr>
<td>2016</td>
<td>9.35</td>
<td>0.053**</td>
</tr>
</tbody>
</table>

Note: * significant at α 5%; ** significant at α 10%

Figure 1. Temporal heterogeneity using a boxplot

Testing for the normality of the residuals of linear regression was conducted based on the Shapiro-Wilk (SW) test. The test results obtained a value of 0.972, with a p-value of 0.000738. This indicates that the distribution of the residuals from the model has not followed
normal distribution. Transformation was made by the Box-Cox method to deal with side abnormalities. The Box-Cox transformation results obtained a minimum lambda value of -0.182. The resulting lambda value is approaching 0, so the transformation used in this study is the function of natural logarithms (ln) in the response variable.

Spatial heterogeneity testing using the Breusch-Pagan test statistic was performed to determine whether there was diversity due to spatial influence. The tests are conducted annually and simultaneously on the 119 regencies/municipalities in Java Island in 2010-2016. The Breusch-Pagan test results are presented in Table 4. These, in combination and annually, are significant at the 5 percent level, apart from 2016, when it is significant at the 10% real level. It can therefore be said that there is spatial heterogeneity in the GRDP construction sector data of the regencies/municipalities in Java Island in 2010-2016. Inequality of spatial diversity is thought to be caused by differences in characteristics in each location.

To ascertain the existence of temporal heterogeneity, the data were described using a boxplot, as shown in Figure 1. The figure shows that the distance between GRDP value quartiles in the construction sector is different each year. This difference illustrates the diversity of data, so it can be said that between years there is such diversity. LnGRDP in the construction sector in Java has spatial, as well as temporal diversity. One of the suitable models to model this in the construction sector in Java Island is the GTWR model.

### 3.2. Geographically and Temporally Weighted Regression (GTWR) Model

The weighting matrix used in the study was the Bisquare weighting function, which produces the same bandwidth in each location. Determination of optimum bandwidth was made by calculating the smallest CV (cross validation) value. This was 411.572, with a spatiotemporal bandwidth value (bST) of 5.518. In addition, the optimum parameter ratio (v) was generated at 0.512, with a spatial distance parameter (λ) of 0.922, and temporal parameter (µ) of 0.472.

#### 3.2.1. Estimator of the parameters of the GTWR model

A description of the parameter estimator using the GTWR method is given in Table 5. The estimator of the parameter intercept in GTWR model, the LnPDRB of the construction sector in Java, ranged from 13.178 to 13.730, or 528606.72 to 918043.45 million rupiahs if there were no changes in the explanatory variables. While the explanatory variables of population (X1), local revenue (X2) and the number of construction establishments (X4) are positive, meaning that if there is an increase in population, local revenue or the number of construction establishments of 1 unit, the value of the GRDP of the construction sector will increase by $e^β_1$, $e^β_2$ or $e^β_4$ times if there is no change in the other explanatory variables. This is inversely proportional to the explanatory variable area (X3) which has a negative value in all regencies/municipalities every year, meaning that an area increase of 1 km² will reduce the value of the construction sector GRDP by $e^β_3$ and if there is no change in the other explanatory variables.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Minimum</th>
<th>Maximum</th>
<th>Mean</th>
<th>Standard Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept</td>
<td>13.178</td>
<td>13.730</td>
<td>13.450</td>
<td>0.158</td>
</tr>
<tr>
<td>Population</td>
<td>7.165×10⁻⁷</td>
<td>1.164×10⁻⁶</td>
<td>8.738×10⁻⁷</td>
<td>1.398×10⁻⁷</td>
</tr>
<tr>
<td>Local Revenue</td>
<td>4.488×10⁻⁸</td>
<td>2.504×10⁻⁷</td>
<td>5.858×10⁻⁸</td>
<td>2.171×10⁻⁸</td>
</tr>
<tr>
<td>Area</td>
<td>-3.048×10⁻⁴</td>
<td>-1.202×10⁻⁵</td>
<td>-2.074×10⁻⁵</td>
<td>5.250×10⁻⁵</td>
</tr>
<tr>
<td>Establishment</td>
<td>1.924×10⁻⁴</td>
<td>7.961×10⁻⁴</td>
<td>5.556×10⁻⁴</td>
<td>1.799×10⁻⁴</td>
</tr>
</tbody>
</table>
3.2.2. Interpretation of the GTWR model

The GTWR model generates different parameter estimating values in each location and year. This is in accordance with the purpose of its use, which is to form a model in each region for every year (Conita & Purwaningsih, 2017). The results of the model can be used to evaluate the policies that have been applied by each regency/municipality. In addition, it can also be used as a basis to decide whether the policies are still relevant or need to be updated. In the GTWR model, each variable has a different effect. Likewise, the magnitude of the parameter coefficient value also varies in each regency/municipality and year.

For example, the GTWR model for Malang Regency in 2015 is as follows:

\[ y = e^{13.31+1.05 \times 10^{-6} x_1 + 8.96 \times 10^{-6} x_2 + 1.47 \times 10^{-4} x_3 + 3.40 \times 10^{-4} x_4} \]

For Malang Regency in 2016 it is as follows:

\[ y = e^{13.35+1.04 \times 10^{-6} x_1 + 6.04 \times 10^{-6} x_2 + 1.43 \times 10^{-4} x_3 + 3.57 \times 10^{-4} x_4} \]

For Malang City in 2015 it is as follows:

\[ y = e^{13.49+9.16 \times 10^{-7} x_1 + 5.40 \times 10^{-6} x_2 + 1.38 \times 10^{-4} x_3 + 3.58 \times 10^{-4} x_4} \]

And for Malang City in 2016 it is as follows:

\[ y = e^{13.58+8.32 \times 10^{-7} x_1 + 5.38 \times 10^{-6} x_2 + 1.35 \times 10^{-4} x_3 + 4.15 \times 10^{-4} x_4} \]

The interpretation of the GTWR model for Malang Regency in 2015 is the estimated value of the construction sector GRDP of \( e^{13.31} \) or 603197.53 million rupiahs if there is no change in the independent variables. If the population of Malang Regency in 2015 increases by 1 person, it will increase the estimated value of construction sector GRDP by \( e^{1.05 \times 10^{-6}} \), or 1.000001 times, if other explanatory variables remain unchanged. The coefficient of the local revenue explanatory variable of \( 8.96 \times 10^{-6} \) explains that the estimated GRDP of the construction sector will increase by \( e^{8.96 \times 10^{-6}} \), or 0.99985006 times, if the population of Malang Regency in 2015 increases by 1 million rupiahs and there is no change in other explanatory variables. If there is no change in the area of Malang Regency in 2015, the estimated GRDP of the construction sector will decrease by \( e^{1.47 \times 10^{-4}} \), or 0.99985006 times, if other explanatory variables do not change, then the estimated value of the GRDP of the construction sector will decrease by \( e^{1.47 \times 10^{-4}} \), or 0.99985006 times, when the number of construction establishments increases by 1 and other explanatory variables are unchanged.

3.2.3. Testing the Parameters of the GTWR Model

Testing of the GTWR model was conducted to establish the explanatory variables that influenced the response variable for each time and location. Most regions have different influential factors, which are because each regency/municipality has different characteristics, both in terms of geography, public facilities, social facilities and government. The differences in influencing factors allow each location to develop its own policies in accordance with the conditions and needs in their respective regions in order to increase the value of construction sector GRDP.

Regency/municipality grouping based on influential factors using the GTWR model is illustrated in Figure 2. In the GTWR model, two groups were formed. The first group was the regencies/municipalities whose construction sector GRDP was influenced by population (X_1), local revenue (X_2) and area (X_3). The second group comprised regencies/municipalities whose construction sector GRDP was influenced by population (X_1), local revenue (X_2), area (X_3) and number of construction establishments (X_4).
Figure 2. Map of regency/municipality distribution based on influencing factors

Table 6. Regency/municipality grouping based on influential factors

<table>
<thead>
<tr>
<th>Year</th>
<th>X₁, X₂, X₃</th>
<th>X₄, X₅, X₆, X₇</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>2010</td>
<td>All regencies/municipalities in Java</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2011</td>
<td>Pamekasan, Sumenep, Lebak</td>
<td>Other regencies/municipalities</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Jombang, Nganjuk, Madiun, Magetan, Sampang, Pamekasan, Surabaya City, Batu City, Lebak, Tangerang</td>
<td>Other regencies/municipalities</td>
<td></td>
</tr>
<tr>
<td>2012</td>
<td>Lumajang, Jember, Jombang, Nganjuk, Madiun, Magetan, Sampang, Pamekasan, Sumenep, Kediri City, Pasuruan City, Mojokerto City, Surabaya City, Batu City, Lebak, Tangerang</td>
<td>Other regencies/municipalities</td>
<td></td>
</tr>
<tr>
<td>2013</td>
<td>Jombang, Nganjuk, Madiun, Magetan, Sampang, Pamekasan, Sumenep, Surabaya City, Batu City, Lebak</td>
<td>Other regencies/municipalities</td>
<td></td>
</tr>
<tr>
<td>2014</td>
<td>All regencies/municipalities in Java</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2015</td>
<td>All regencies/municipalities in Java</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2016</td>
<td>All regencies/municipalities in Java</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Details of the regency/municipality groupings based on influential factors are presented in Table 6. The table shows that all regencies/municipalities in Java had the same influential factors in 2010, 2015 and 2016. Changes occurred in 2011-2014, when the explanatory variable of the number of construction establishments was not significant in several regencies/municipalities.

4. Conclusion

The factors that affected the GRDP of the construction sector varied amongst the regencies/municipalities in Java in the period 2010 to 2016; this can be used as material for policymaking and evaluation in accordance with the differing influential factors. The explanatory variable of population has a positive and significant effect. We know that humans need facilities that must be built to support their lives; increasing population in an area will require many such facilities.

The explanatory variable of local revenue also has a positive and significant effect. The construction of facilities built by local governments involves use of the Regional Revenue and Expenditure Budget, part of which is local revenue. So if a local government wants to increase the construction of facilities for the community, it is also necessary to increase local revenue as a source of development. The explanatory variable of area has a negative effect on each regency/municipality and in each year. The smaller the area, the easier the access between regions, meaning development is faster and that there is an increase in the GRDP of the construction sector.

The explanatory variable of the number of construction establishments have a positive effect on each regency/municipality each year. However, in 2012-2014 some regencies/municipalities did not see a significant effect. The increasing number of construction companies is expected to significantly increase the GRDP of the construction sector, but in some regencies/municipalities this has no significant effect; for example, Sampang Regency, which has a large number of companies that made no significant contribution to increasing construction sector GRDP. The ease of obtaining permission to establish a company is unable to increase the GRDP of the construction sector.

Acknowledgments

We would like to acknowledge BPS-Statistics Indonesia for data and funding support, both thesis mentors for their supporting knowledge, and all the team at the Statistics Department of IPB University.

References


